

High Precision Results from Numerical Simulations of Quantum Chromodynamics

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The Standard Model

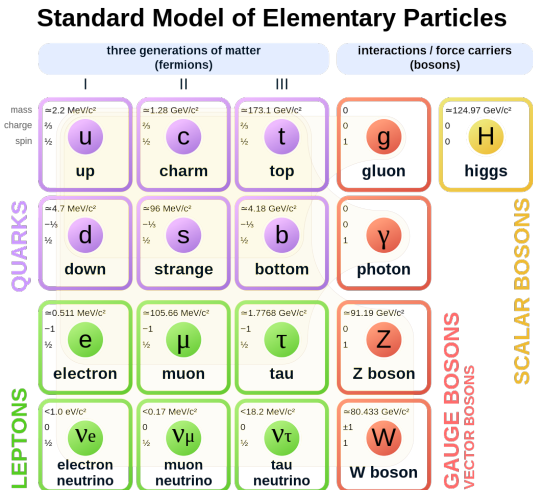


Fig.: [Wiki]

The Standard Model

Matter particles (spin $S = 1/2\hbar \rightarrow$ fermions)

- quarks: "up" (u), "charm" (c) und "top" (t), "down" (d), "strange" (s), "bottom" (b)
 \rightarrow masses: $m_u = 2.3\text{MeV}/c^2$ (up quark), ..., $m_t = 173\text{GeV}/c^2$ (top quark)
- leptons: electron (e^-), muon (μ^-), tau (τ^-), electron neutrino (ν_e), muon neutrino (ν_μ), tau neutrino (ν_τ)

Interaction particles (spin $S = 1\hbar \rightarrow$ bosons)

- there are (only) 4 fundamental forces (with associated interaction particles):
 - electromagnetic force (photon γ)
 - strong force (gluons g)
 - weak force (W^\pm, Z^0 bosons)
 - gravitational force (graviton G (?)) \leftarrow not included in the Standard Model

Bound states

Quarks can form bound states (due to the strong force)

- baryons (consist of 3 quarks: $q_1 q_2 q_3$):
 proton p (uud), neutron n (udd), lambda Λ (uds), sigma Σ^+ (uus), xi Ξ^- (dss), omega Ω (sss),...
- mesons (consist of quark and anti-quark: $q_1 \bar{q}_2$): pion π^+ ($u\bar{d}$), kaon K^+ ($u\bar{s}$)
- ...

\Rightarrow masses can be calculated numerically \leftarrow part of this project (focus on strong force + light quarks (up, down, strange, charm)) S

Physics of the Standard Model

Physics of the Standard Model

- (almost too) perfect agreement of experimental results and theoretical predictions within the Standard Model
- BUT, there are good reasons to believe that the Standard Model is incomplete
 - e.g., it is not known how to include gravity in the Standard Model consistently
- ongoing search for little deviations from experiment results and theoretical predictions
- such deviations may hint how to extend the Standard Model
- ⇒ high precision is needed in both experiments and theoretical predictions

At Regensburg: focus on physics related to the strong force

- theoretical calculations at Regensburg performed both numerically and analytically
- numerical projects at Regensburg:
 - light baryon spectrum/scale setting
 - heavy baryon spectrum
 - pseudoscalar decay constants (+ charm), charmonium resonances
 - quark masses (+ charm)
 - η/η' -mixing
 - hadron structure: baryon charges, form factors, TMD, MDA/BDA, DPD, LECs
- ⇒ goal: high precision results from numerical calculations

Remark: numerical simulations are also very important for quantities where accessibility w.r.t. other methods is limited

Numerical Simulations of the Strong Force

Theory of the Strong Force = Quantum Chromodynamics (QCD)

- QCD is a non-linear theory
→ many important quantities can only be calculated numerically
- only ab-initio framework known for numerical simulations of QCD → Lattice QCD

Lattice QCD

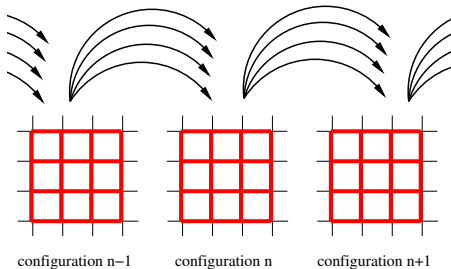
Algorithm: Hybrid Monte Carlo (HMC)

- Generate ensembles by a Langevin-type algorithm (stochastic differential equation)
- evolve along classical trajectory:
→ integration along extra dimension (simulation time)
- solve equation of motion of 5-dim. Hamiltonian

Ensembles ← calculation of observables

- ⇒ each ensemble consists of several configurations
- ⇒ single config. = 4d lattice grid (with lattice spacing a)
- on each site: 4×9 complex numbers
- 4d = 3 spatial + 1 temp. directions (volume = $L^3 \times T$)

classical trajectories



Simulation Overview

Simulation details

- due to computational costs → simulations are performed mostly at
 - larger quark than physical quark masses
 - rather coarse lattice spacing
 - not too large finite volume
- in addition approximation are made: light quark mass $m_\ell = m_{up} \approx m_{down}$, heavier quarks (charm and heavier) are not simulated, no electromagnetic contributions included (also weak force neglected)
 - reasonable assumptions w.r.t. precision reached at state of the art lattice QCD simulations
- ⇒ however, we need to take the following limits to obtain physical results
 - chiral extrapolation: light and strange quark mass $m_\ell \rightarrow m_{\ell,physical}$ $m_s \rightarrow m_{s,physical}$
 - continuum extrapolation: lattice spacing $a \rightarrow 0$
 - (spatial) volume $V_S \rightarrow \infty$

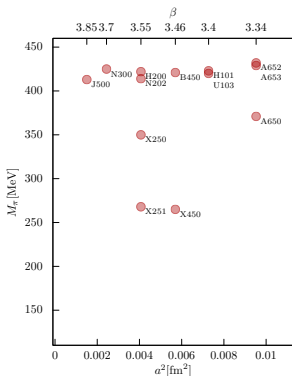
CLS 2 + 1f simulation program

→ see <https://www-zeuthen.desy.de/alpha/public-cls-nf21/>

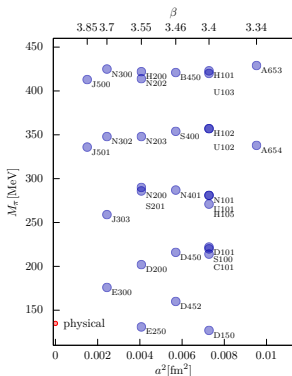
Such simulations are a large scale project → ongoing for more than 10 years now

- large collaboration → CLS (Coordinated Lattice Simulations): HU Berlin, CERN, TC Dublin, Krakow, UA Madrid, Mainz, Milano Bicocca, Münster, Odense/CP3-Origins, Regensburg, Roma I, Roma II, Wuppertal, DESY Zeuthen
- ⇒ main focus of this large scale project: performing a well controlled continuum limit

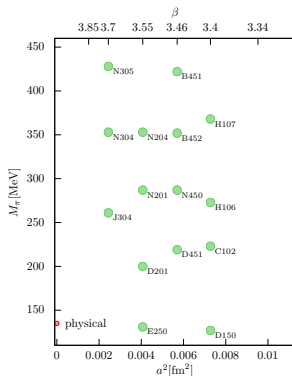
Ensemble Overview



$$m_s = m_\ell$$



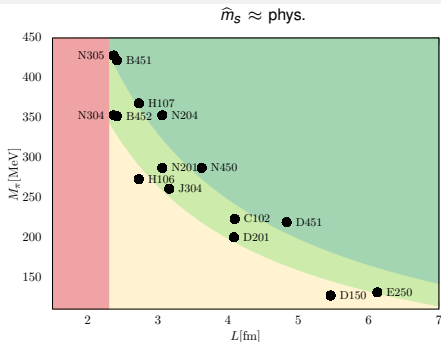
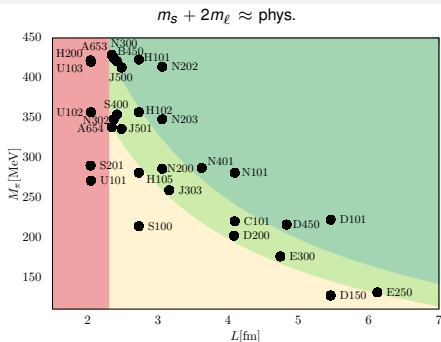
$$m_s + 2m_\ell \approx \text{phys.}$$



$$\hat{m}_s \approx \text{phys.}$$

- simulations are performed at unphysical light and strange quark masses m_ℓ , m_s and at finite lattice spacing a
 → extrapolation to physical quark masses and zero lattice spacing necessary!
 → computational costs increase drastically along these limits!
- 6 different lattice spacings ($a \approx 0.098 - 0.039$ fm), 2 ensembles at the physical point
- geometries range from 48×24^3 to 192×96^3

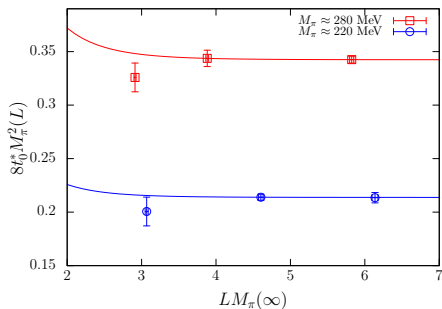
Finite volume effects ← this project



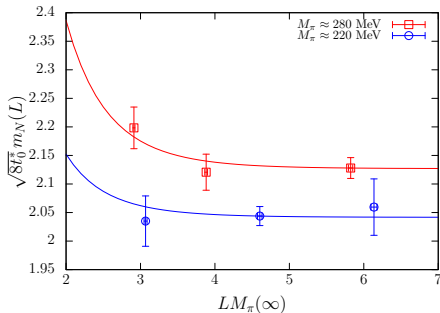
Finite volume effects in Lattice QCD

- remove finite volume effects → take the limit of infinite spatial volume $V_S = L^3$ ($L \rightarrow \infty$)
- finite volume effects are dictated by pion mass M_π and L
- yellow area: $M_\pi L \leq 4$
- light green area: $4 < M_\pi L \leq 5$
- green area: $5 < M_\pi L$
- almost all ensembles are within light green or green area (and also $L \gtrsim 2.3$ fm)
→ small finite volume effects

Finite volume effects ← this project



pion mass

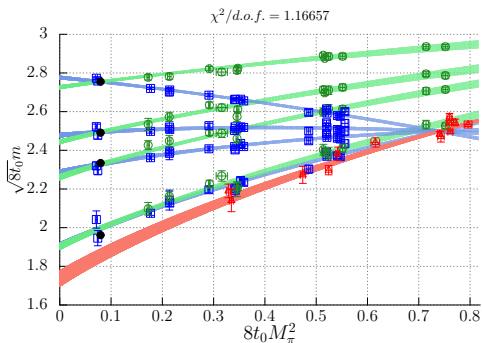


nucleon mass

Dedicated ensembles with small/large volumes ← additional ensembles currently generated within this project

- small finite volume effects for $m_\pi L > 4$
- given the large number of ensembles, small effects add up!
 - include finite volume effects for baryons in fits: quality of fits increases significantly ($\chi^2/dof \sim 1.4 \rightarrow 1.2$)
 - finite volume effects are relevant and a good understanding of these effects is needed
 - ⇒ detailed investigation of finite volume effects needed ← this project (results in progress)

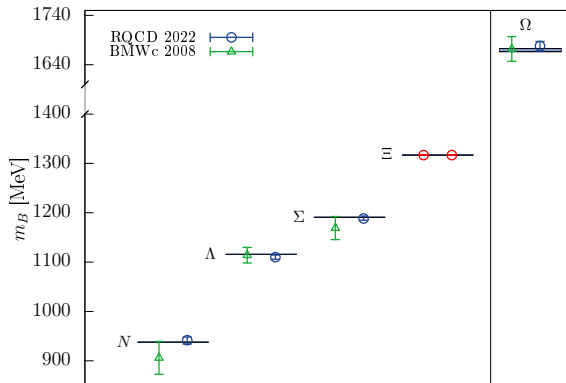
Chiral and Continuum Extrapolation Baryon Spectrum



Extrapolation in lattice spacing a (continuum limit) and quark masses m_ℓ, m_s (chiral limit)

- baryon masses m : nucleon (N), lambda (Λ), sigma (Σ), xi (Ξ), black points=physical values
- combined chiral and continuum fit
→ visualized here: only extrapolation to physical light quark mass $m_\ell \rightarrow m_{\ell,physical}$
- note: pion mass $M_\pi^2 \sim m_\ell$: $m_\ell \rightarrow m_{\ell,physical} \longleftrightarrow M_\pi^2 \rightarrow M_{\pi,physical}^2 \approx 135\text{MeV}/c^2$

Light Baryon Spectrum



Results of fits for masses of baryons: nucleon (N), lambda (Λ), sigma (Σ), xi (Ξ), omega (Ω)

- comparison of previous results from BMWc collaboration from 2008 and our recent results (RQCD 2022)
- black horizontal lines represent experimental data

Lattice QCD: Hard- and Software

Hardware

- JURECA-BOOSTER@Jülich: Intel KNL
- JUWELS@Jülich: Intel Skylake
- JUWELS-BOOSTER@Jülich: Nvidia A100
- SuperMUC-NG@Munich: Intel Skylake
- QPACE3@UR: Intel KNL
- QPACE4@UR: ARM (Fujitsu A64FX)
- FRITZ@FAU

Storage and data management: Peta Bytes of data

- 126,000 configurations (975 TB) stored at Zeuthen and redundantly at Regensburg (on tape)
- analysis files stored at Regensburg \sim 1.2 PB and a lot a JSC
- tools are available for backing up data (reading and writing to tape), scripts are used for automated data handling
- configurations are available for users outside CLS upon request

Software

- C/C++, Python
- high performance solver: multigrid solvers (DD- α AMG, IDFLS)
- software packages: openQCD, Chroma, GRID + GPT (open source)

Summary

Standard Model

- excellent agreement of experimental and theoretical results
- Standard Model is believed to be incomplete
→ search for little deviation from the Standard Model
- high precision results needed in both experiments and theory

This project

- high precision results from Lattice QCD necessary
 - need to control all systematic uncertainties in Lattice QCD simulations
 - finite volume effects is a relevant source of systematics at the precision reached now
→ see calculated baryon masses
- ⇒ a good understanding of finite volume effects is needed
- ⇒ fritz@fau: perfect environment to perform this important, intermediate scale project