THE COMEDY CLUB OF HIGH-PERFORMANCE COMPUTING: LOW-RANK MATRIX APPROXIMATION TAKES THE STAGE!

KAUST

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Extreme Computing Research Center

NHR PerfLab Online Seminar May 16th 2023

NHR

IFAU

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HPC Comedy Club



Intel #97



IBM/NVIDIA CPU/GPU #4



AMD #27



Fujitsu ARM A64FX #2

HPC Comedy Club



Intel #97



IBM/NVIDIA CPU/GPU #4





NEC



AMD #27



Fujitsu ARM A64FX #2

HPC-AI Comedy Club



Intel #97



IBM/NVIDIA CPU/GPU #4



FUJITSU

NEC

GRAPHCORE





AMD #27



Fujitsu ARM A64FX #2



جامعة الملك عبدالله للعلوم والتقنية King Abdullah University of Science and Technology



SHAHEEN III KEY FACTS

Shaheen III supercomputer with 25 HPE Cray EX supercomputer cabinets

Expected to deliver over 100 Pflops/s

20x faster than Shaheen II

4,608 CPU compute nodes, AMD EPYC[™] processors, "Genoa", amounting to 884,736 cores in the entire system

2,800 NVIDIA Grace Hopper Superchips, tightly coupled CPU/GPU accelerators Cray Slingshot interconnect

Cray ClusterStor E1000 with additional 50 PB of storage capacity

Operational by end of 2023

Accelerating research and developments in energy, environment, food, water and healthcare

2/3rds of KAUST faculty use computational modeling and simulation: **"to outcompute is to outcompete"**

Hardware Landscape





AMD Epyc Genoa

High cache capacity High memory bandwidth x86 programming env Memory-bound workloads NVIDIA Grace Hopper

High speed CPU-GPU interconnect Memory coherency Support for mixed precisions Compute-bound workloads

Hardware Landscape









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Cerebras WSE-2 2.6 Trillion Transistors 46,225 mm² Silicon

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Al-focused chip Flat memory hierarchy High SRAM bandwidth Inference

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How do we reconcile this hostile environment with HPC scientific applications?

10 **Revisiting the Hourglass** A x = bmany apps **ECRC** is right common infrastructure here many @KAUST_ECRC archs https://www.facebook.com/ecrckaust

Reshaping Linear Algebra for Massively Parallel Architectures

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- Enhance user-productivity using layers of abstraction
- Expose parallelism using fine-grained computations
- Achieve scalability using asynchronous executions
- Exploit data sparsity using low-rank approximations
- Maintain code portability using standard basic blocks

Are you willing to redesign your algorithm? One possible productive solution: Matricization



Fig. 4: Left: Soil moisture residuals at the topsoil of the Mississippi River basin. Right: Wind speed (m/s) in the Arabian Sea.

3D Geospatial Statistics



3D Mesh Deformations



Seismic Imaging



3D Computational Electromagnetics



Wireless Communications





Fig. 4: Left: Soil moisture residuals at the topsoil of the Mississippi River basin. Right: Wind speed (m/s) in the Arabian Sea.

3D Geospatial Statistics

GAUSS Award 3D Computational Electromagnetics COVID19 Structure from PDB



3D Mesh Deformations



Seismic Imaging



Wireless Communications Best Paper PASC'18 E-ELT, VLT, and Subaru Telescopes





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3D Geospatial Statistics



IEEE IPDPS'23 Springer ISC'23

ACM TOPC'21

IEEE IPDPS'22

3D Mesh

Deformations

Communications



Seismic Imaging





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Wireless Communications



Supporting Several Major Ground-Based Telescopes



THE VERY LARGE TELESCOPE



THE EUROPEAN EXTREMELY LARGE TELESCOPE



THE SUBARU TELESCOPE

Supporting Several Major Ground-Based Telescopes

SCEXAO THE SUBARU CORONOGRAPHIC

EXTREME AO



MAVIS MCAO ASSISTED VISIBLE IMAGER AND SPECTROGRAPH



THE VERY LARGE TELESCOPE

EPICS EXOPLANET IMAGING CAMERA AND SPECTROGRAPH

> MAORY MULTI-CONJUGATE ADAPTIVE OPTICS RELAY

MICADO MULTI-ADAPTIVE OPTICS IMAGING CAMERA FOR DEEP OBSERVATIONS



THE EUROPEAN EXTREMELY LARGE TELESCOPE



THE SUBARU TELESCOPE

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The Atmospheric Turbulence



The sun observed with a compact camera

- Disturbs the trajectory of light rays
- Reduces astronomical images quality

Adaptive Optics for Giant Telescopes

Control in real-time the shape of the incoming wavefront

- Sensors are cameras equipped with an optical device (lenslet array, pyramidal prism, etc...)
- **Deformable mirrors** to compensate for wavefront distortions
- Typical rate of operation is 1kHz
- Compute pipeline latency below
 1 millisecond
- Stable time-to-solution is critical to ensure stable operations (jitter of the order of 10s of µs)
- Matrix-Vector Multiplication (MVM)
 is the most critical computational kernel



One of The Key Hardware Components: The Deformable Mirrors

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MAVIS in a nutshell

Flagship 3rd-generation instrument for the Very Large Telescope

- Imager & Spectrograph fed by Multi-Conjugate AO
- Scaling up the whole AO concept:
 - More actuators
 - Faster control system
 - Exquisite calibrations
- Fast-track project:
 First-light by 2026
- **Deeper & Sharper** than any space-based instrument



Rank Analysis of the Tomographic Reconstructor

Splitting the matrix into tiles and looking at ranks

- Tiles size aligned with system parameters
- Data sparse, opportunity for low-rank matrix approximations













TLR-MVM

4) Translate Yv (V bases) to Yu (U bases)



TLR-MVM

5) Calculate y = U . Yu







Numerical Accuracy Assessment on MAVIS Datasets

[%]

Strehl Ratio

31

Speedup and Strehl Ratio VS Compression Parameters



Hardware/Software Specifications³²

Vendor	Intel	AN	ſD	Fujitsu	NVIDIA	NEC
Family	Cascade	EPYC	Instinct	Primergy	Ampere	SX-Aurora
	Lake	Rome		A64FX	GPU	TSUBASA
Model	6248	7702	MI100	FX1000	A100	B300-8
Node(s)/Card(s)	1	1	1	16	1	8
Socket(s)	2	2	N/A	4	N/A	N/A
Cores	40	128	7680	48	6912	8
GHz	2.5	2.2	1.5	2.2	2.6	1.6
Memory	384GB DDR4	512GB DDR4	32GB HBM2	32GB HBM2	40GB HBM2e	48GB HBM2
Sustained BW	232GB/s	330GB/s	1.2TB/s	800GB/s	1.5TB/s	1.5TB/s
LLC	27.5MB	512MB	8MB	32MB	40MB	16MB
Sustained BW	1.1TB/s	4TB/s	3TB/s	3.6TB/s	4.8TB/s	2.1TB/s
Compiler	Intel compiler 19.1.0	GCC compiler 8.2.0		Fujitsu compiler 4.5.0	NVCC 11.0	NEC compiler 3.1.1
BLAS library	Intel MKL 2020	BLIS 3.0.0		Fujitsu SSL II	cuBLAS 11.0	NEC NLC 2.1.0
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x86 MPI + OpenMP

Hardware/Software Specifications³⁴

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ARM MPI + OpenMP

Hardware/Software Specifications³⁵

		() ()				
Vendor	Intel	AN	1D	Fujitsu	NVIDIA	NEC
Family	Cascade	EPYC	Instinct	Primergy	Ampere	SX-Aurora
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Accelerators ROCm / CUDA

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Vector MPI + OpenMP

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- IOD = "I/O Die" doing all the memory/PCI/other socket traffic
- CCD = "Core Compute Die", a chiplet having compute cores only
- CCX = "Core Compute CompleX", a set of cores sharing a L3 cache



Sustained Bandwidth on Synthetic Datasets



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Roofline Performance Model



Performance Across AMD x86 Generations



The Case for Mixed Precisions

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Data transactions with AO hardware rely on UINT16

- WFS cameras provide 12-16 bits data stream as input
- Deformable mirror actuators are controlled through a set of UINT16 commands



MAVIS Instrument







Fig. 4: Left: Soil moisture residuals at the topsoil of the Mississippi River basin. Right: Wind speed (m/s) in the Arabian Sea.

3D Geospatial Statistics



3D Mesh Deformations



Seismic Imaging



3D Computational Electromagnetics



Wireless Communications



Powering Seismic Redatuming w/ TLR-MVM

Seismic redatuming is an important technique to get insights from the Earth's subsurface.

This requires solving an inverse problem. Traditionally, due to computational challenges, only the adjoint is applied.

Some latest research show an alternative method to improve the solution of inverse problems by using an iterative solver, e.g., conjugate gradient iterative solver. This comes at the cost of evaluating multiple expensive MVM operations, as shown in the following equations:

$$\mathbf{x} = \mathbf{R}^{H} \mathbf{y} : \quad x(t, \mathbf{x}_{R}, \mathbf{x}_{A}) = \mathcal{F}_{\omega_{max}}^{-1} \left(\int_{\delta \mathbb{D}} R^{*}(\omega, \mathbf{x}_{B}, \mathbf{x}_{R}) \mathcal{F}_{\omega_{max}} \left(y(t, \mathbf{x}_{B}, \mathbf{x}_{A}) \right) d\mathbf{x}_{B} \right),$$
$$\mathbf{y} = \mathbf{R} \mathbf{x} : \quad y(t, \mathbf{x}_{B}, \mathbf{x}_{A}) = \mathcal{F}_{\omega_{max}}^{-1} \left(\int_{\delta \mathbb{D}} R(\omega, \mathbf{x}_{B}, \mathbf{x}_{R}) \mathcal{F}_{\omega_{max}} \left(x(t, \mathbf{x}_{R}, \mathbf{x}_{A}) \right) d\mathbf{x}_{R} \right).$$





Powering Seismic Redatuming w/ TLR-MVM

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We use tile low-rank matrix-vector multiplication (TLR-MVM) to address the complexity bottleneck.



Threshold ϵ , tile rank: k







Receivers

...

L1 ordering

Sources

Hilbert ordering

SEG/EAGE Overthrust Model

Jointly developed between the Society of Exploration Geophysicists (SEG) and the European Association of Geo- scientists and Engineers (EAGE)

- 3D Geological open model
- 3 x 5 x 2.3 km³
- 217 imes 120 sources
- 177×90 receivers
- 230 complex-valued frequency matrices of size 26040 imes 15930

Numerical Accuracy

Bad

Checking the traces of 8 receivers

Accuracy Threshold: 1e-4

Numerical Accuracy

Post-acquisition processing powered by TLR-MVM to remove free-surface related effects

Summary

- Algorithms first!
- Low-rank matrix approximations are key for solving challenging scientific problems at scale
- Reconciling HPC workloads with the hostile hardware landscape
- Steering AI-focused hardware for HPC scientific applications is worth exploring (*ISC23 paper presentation*)
- Exploiting cache size and leveraging its high bandwidth

We are recruiting!

THANK YOU!

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